

# Small Area Estimation and mapping of poverty in Uganda

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# Profile

## Background



## • Recent Research Projects:

Measurement of material deprivation

Malnutrition in Sub-Saharan Africa

Housing affordability and housing deprivation



## • Teaching:

Quantitative Methods for Social Scientists

Social Policy



# What this talk is about



- Share findings from an empirical example (Small Area Estimation of multidimensional poverty in Uganda)
- Walk you through (some of) the practicalities of doing Small Area Estimation
- Understand the workflow of Small Area estimation to avoid over-reliance on pre-packaged Small Area estimation programs (i.e. what's under the bonnet?)
- The presentation assumes basic understanding of linear regression modelling

# What this talk is not about



- Not an in-depth class on the mathematics behind Small Area Estimation
- Not a series of simulations with some conclusions about which SAE estimator is better
- Not a class on Bayesian Hierarchical modelling

# Outline

- Small Area Estimation in theory
- Small Area Estimation in practice
- Applied example

# Small area estimation

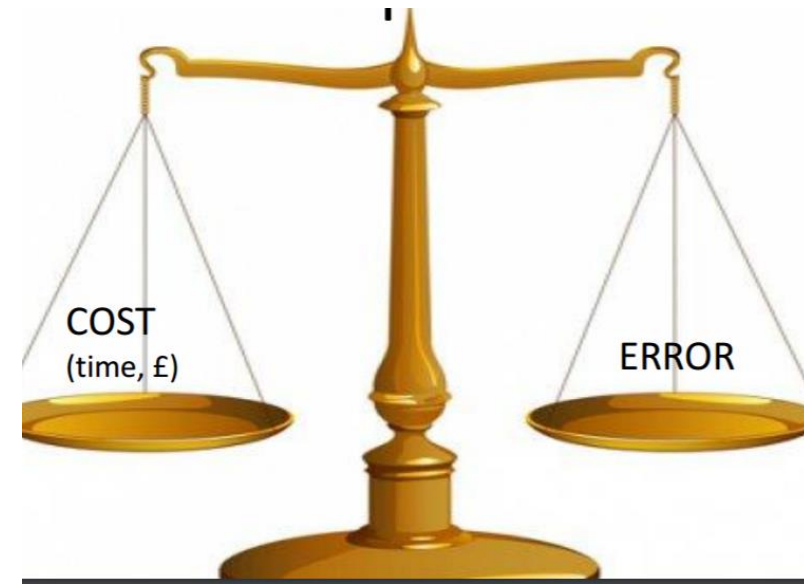
- A set of methods aimed at measuring poverty at local level
- Important for:
  - Funds-allocation
  - Assessment of policies (“No one left behind”)
  - Poor areas within richer regions
  - Influence of place on individual outcomes

# Direct estimates of local poverty

- Margin of error of Proportion  $1.96 \times \sqrt{\frac{\text{Proportion} (1-\text{Proportion})}{\text{number of valid respondents}}}$
- Number of cases needed to achieve a certain Margin of Error for a given proportion:

$$n = \frac{1.96^2 \times \text{Proportion} \times (1-\text{Proportion})}{\text{MoE}^2}$$

- MoE of small-area estimates too high
- Many small areas often not covered at all!



# Example: Uganda

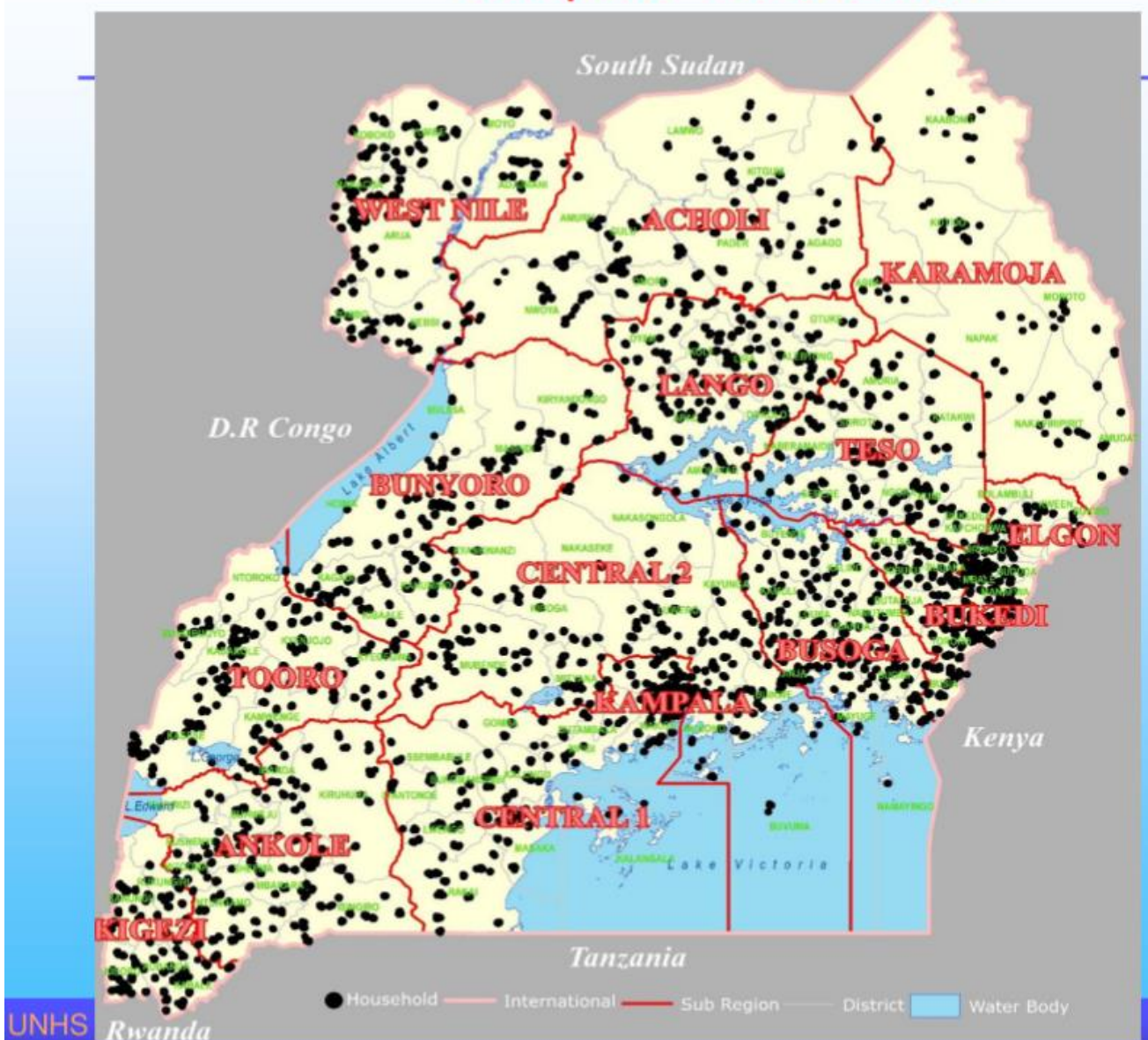
## ➤ Example: Uganda administrative boundaries example

- **Region** > sub-region > district > county > sub-county > parish > enumeration area
- Can we produce sub-county level estimates of poverty using the National Household Survey?





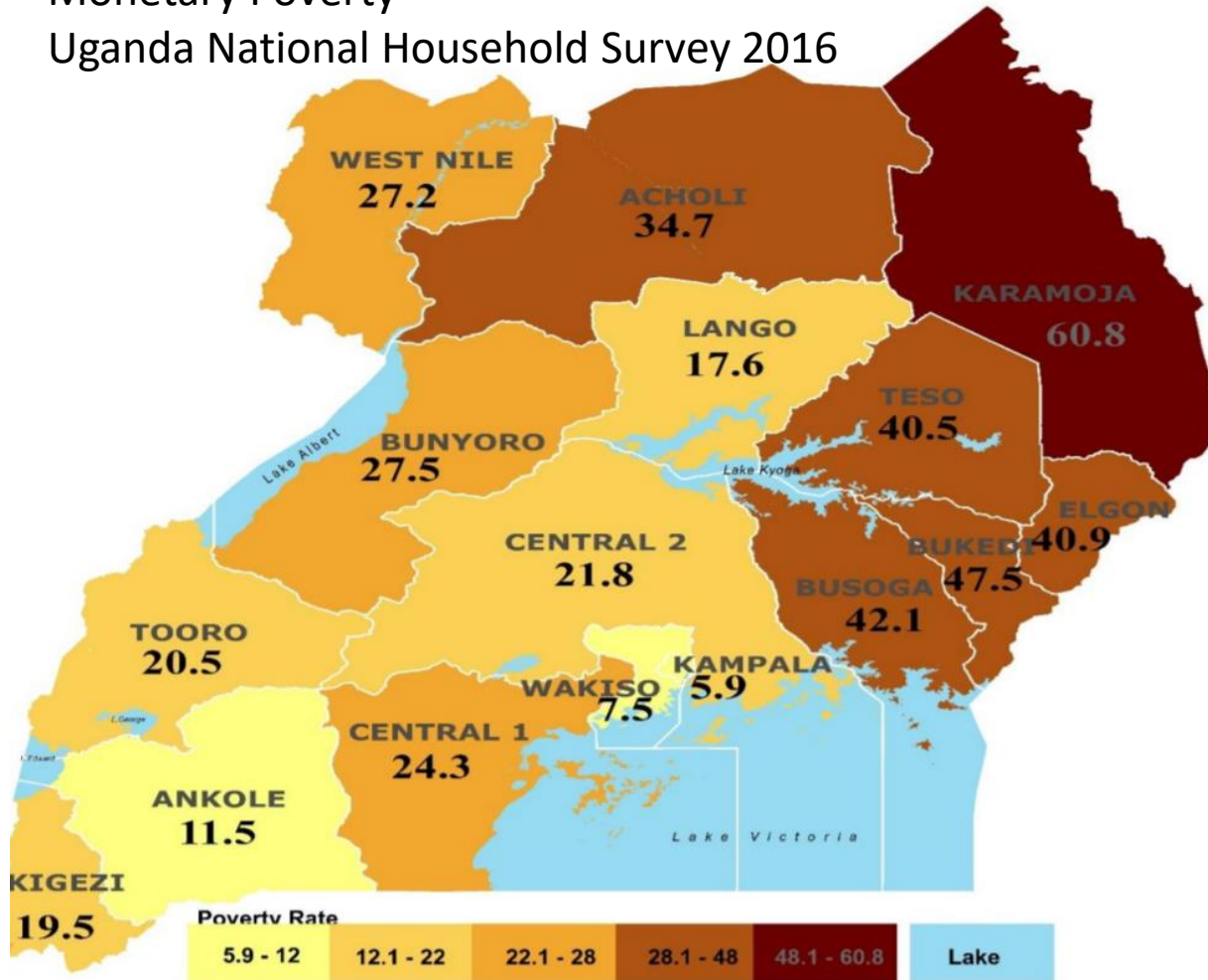
# Distribution of 2016/2017 UNHS sampled households



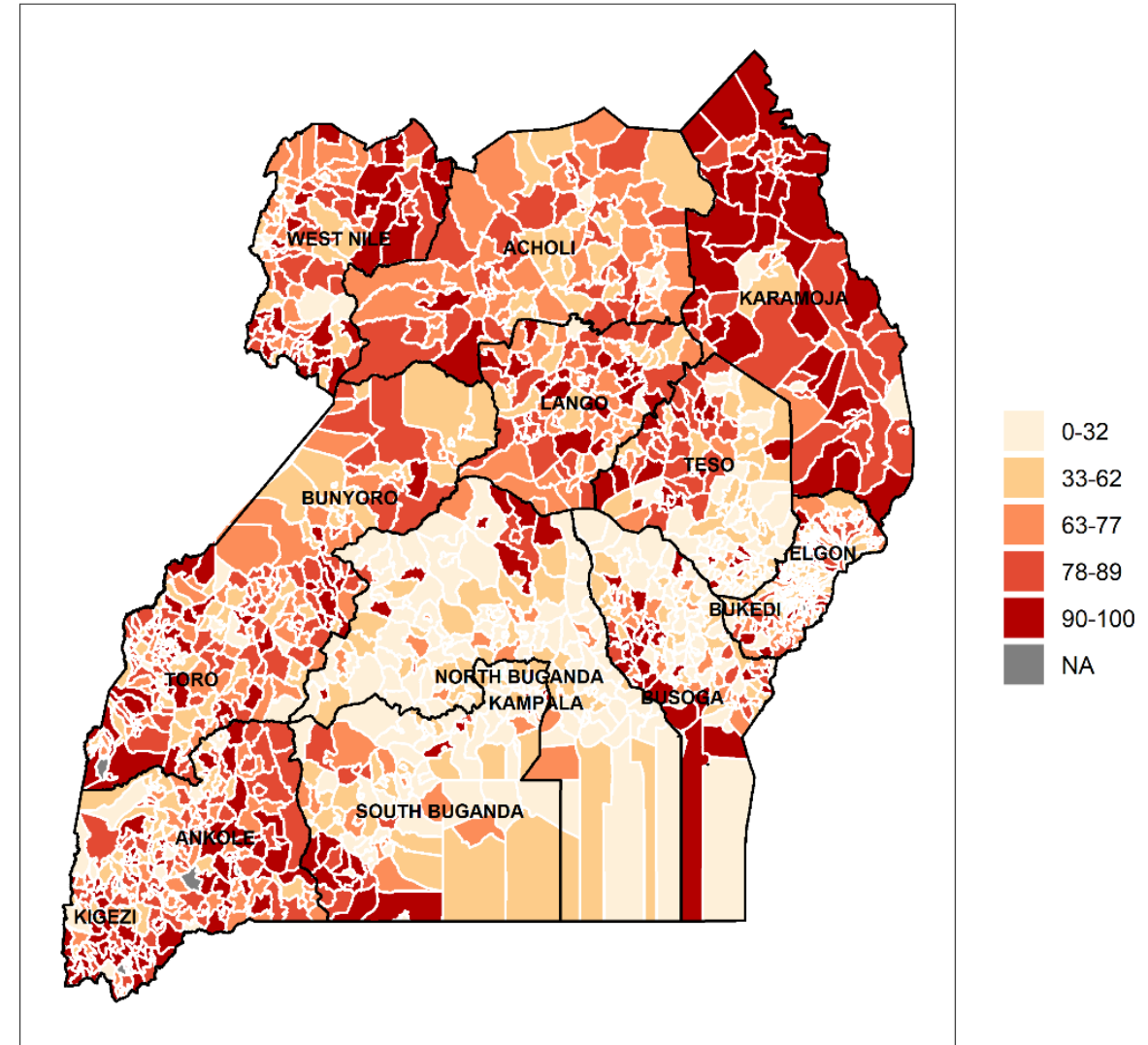
# Poverty Estimates

Monetary Poverty

Uganda National Household Survey 2016



% of households experiencing wall deprivation  
(Subcounty Census Estimates)



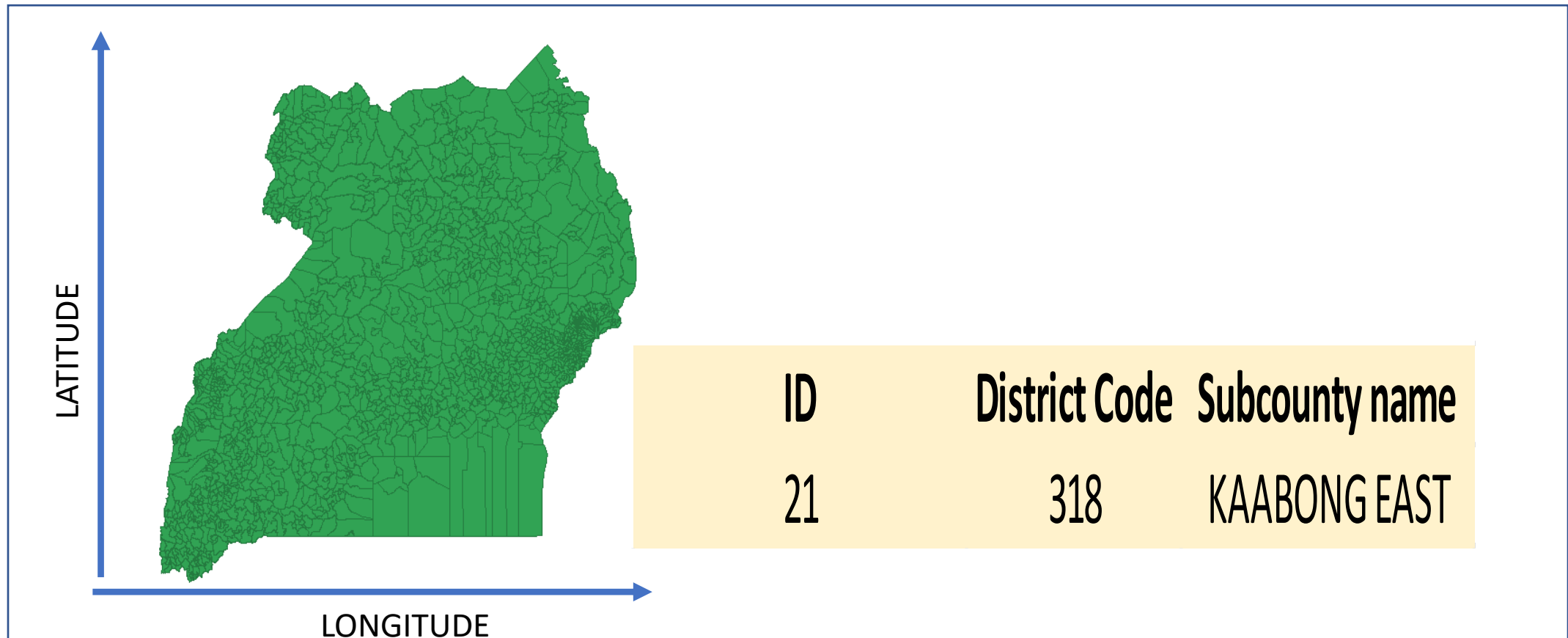
# Small Area Estimation: Basic intuition

- Survey data: More questions, more frequent, fewer cases
- Census data: More cases, fewer questions, less frequent

SAE: Combine strengths to obtain small area estimates

# The Third Dataset

- Your small area Shapefile/s. Just as important as survey and Census



See IPUMS repository <https://international.ipums.org/international/gis.shtml>

# Indirect estimators

- Statistical Modelling

e.g. Multilevel regression modelling (Frequentist or Bayesian)

- Spatial Microsimulation

Involves creation of synthetic micro-population or reweighting using Census area level benchmarks

# Borrowing strength (Individual level modelling)

## Simple Regression Framework example

$$Y_i = \alpha_0 + \beta_1 X1_i + \beta_2 X2_i + e_i$$

$$\text{Income}_i = \alpha_0 + \beta_1 \text{Secondary Education}_i + \beta_2 \text{Urban}_i + e_i$$

$$\text{Income}_i = 50 + 150_1 \text{Secondary Education}_i + 3 \text{Urban}_i + e_i$$

	Income	Has Secondary Education	Lives in Urban area	Survey model predicted Income	Residual
Survey Respondent 1	213	Yes	Yes	50+150+3=203	10
Survey Respondent 2	10	No	No	50	-40

# Borrowing strength (individual level modelling)

SURVEY

Income<sub>i</sub> = 50 + 150<sub>1</sub> Secondary Education<sub>i</sub> + 3 Urban<sub>i</sub> **Survey data model estimates**

	Income	Has Secondary Education	Lives in Urban area	Survey model predicted Income	Residual
Survey Respondent 1	213	Yes	Yes	50+150+3=203	10
Survey Respondent 2	10	No	No	50	-40

CENSUS

	Income	Has Secondary Education	Lives in Urban area	Survey model predicted Income
Census Respondent 1	Not collected	Yes	Yes	50+150+3=203
Census Respondent 2	Not collected	No	No	50

# Poverty SAE models

Most widespread methodologies in poverty SAE:

- Fay-Harriot
- ELL/World Bank
- Empirical Bayes
- Hierarchical Bayes



# Borrowing strength- Multilevel modelling

## Simple Regression Framework example

$$\text{Income}_i = \alpha_0 + \beta_1 X_{1i} + e_i \quad \text{Survey data model (example with just one independent variable)}$$

## Multilevel Framework

$$\text{Income}_{ij} = \alpha_{0j} + \beta_{1j} X_{1ij} + \varepsilon_{ij}$$

$$\alpha_{0j} = \gamma_{00} + \gamma_{01} W_j + \mu_{0j}$$

$$\beta_{1j} = \gamma_{10} + \gamma_{11} W_j + \mu_{1j}$$

# Borrowing strength (individual level modelling)

SURVEY

$$\text{Income}_{ij} = \alpha_j + \beta_1 X_{1ij} + \varepsilon_{ij}$$

$$\alpha_j = \gamma_{00} + \gamma_{01} W_j + \mu_j$$

CENSUS

	Income	Has Secondary Education	Lives in Urban area	Survey model predicted Income
Census Respondent 1 in <u>Busaana</u>	Not collected	Yes	Yes	50+150+3+ $\mu_{\text{BUSAANA}}$
Census Respondent 2 in <u>Busaana</u>	Not collected	No	No	50+ $\mu_{\text{BUSAANA}}$

# Small Area Estimation in practice

# Pre-modelling choices: Which small area?

- Choose your target levels (your “Small Area”).

Uganda 2016 example:

- **Region** > **sub-region** > **district** > **county** > sub-county > **parish** > **enumeration area**

# Pre-modelling checks: Survey and Census data Comparison

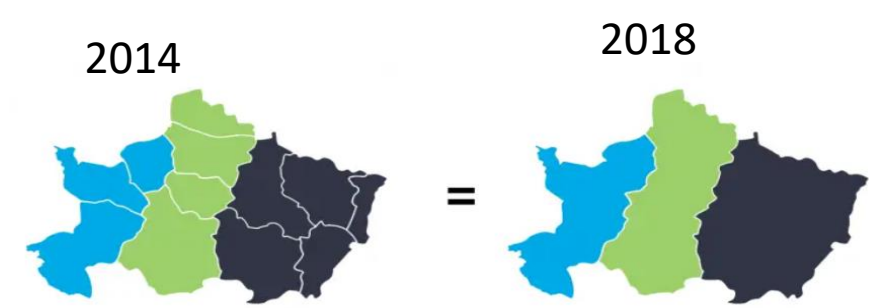
## **1) Check**

- Check that the distribution of your dependent and independent variables match in sample and Census
- How do they derive household size?
- How is the household head selected?

## **2) Inform variable selection and possible post-stratification**

Do differences between Census and survey reflect genuine differences or sampling error and/or measurement error and/or nonresponse error?

# Pre-modelling choices: boundaries



- 1) Identify a consistent and relevant nesting structure of geographical boundaries. Choose your target level (your “Small Area”)
- 2) Establish that this is consistent in both survey, Census data and shapefile.
- 3) Research changes in boundaries between Census and survey
- 4) Establish a strategy to update Census and Survey boundaries and create updated geography variables and shapefiles.
- 5) Create a unique ID in your (GIS) shapefile and then match it to your survey and Census data

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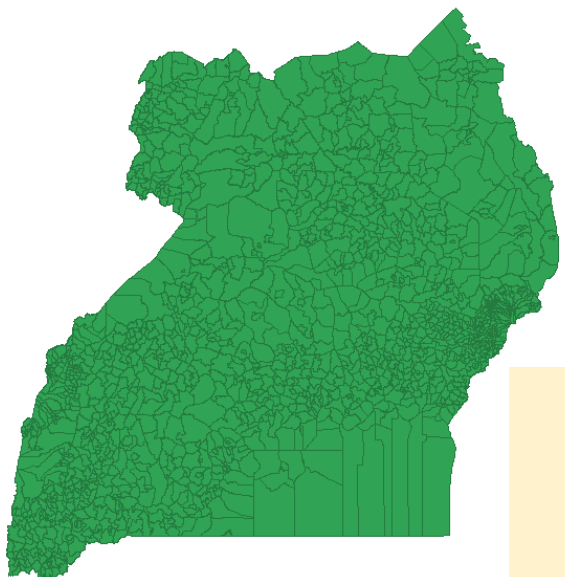
### SURVEY

District Code	Subcounty name	Shapefile subcounty ID
318	KAABONG EAST	21

### CENSUS

District Code	Subcounty name	Shapefile subcounty ID
318	KAABONG EAST	21

### SHAPEFILE

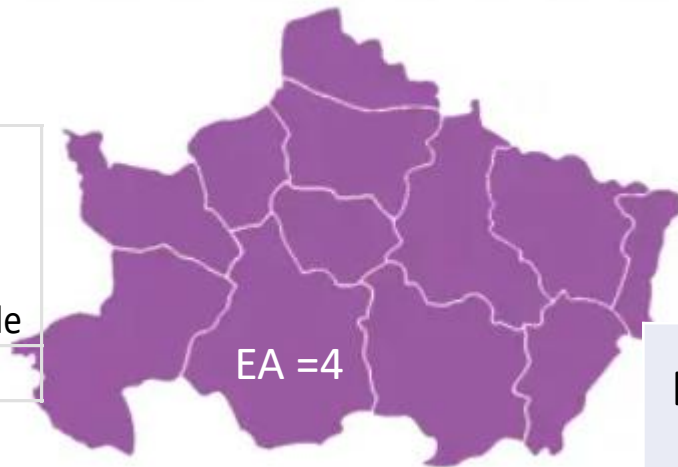


ID	District Code	Subcounty name
21	318	KAABONG EAST

5) If the match is not complete, try to match on the lowest-level area available in shapefiles and datasets (e.g. enumeration areas).

## SURVEY

District Code	Subcounty name	EA name	EA code
318	NA	KALODEKE	4



*shapefile*

## CENSUS

District Code	Subcounty name	EA name	Subcounty name
318	NA	KALODEKE	4



5) If matching is not complete...persevere and eventually triangulate, inspect manually etc....

## SURVEY

District Code	EA name	EA code	Shapefile subcounty ID
318	KALODEKE	4	21
318	SOKODU B	8	22
318	KOBUIN_a	11	?



## CENSUS

District Code	EA name	Shapefile subcounty ID
318	KALODEKE	21
318	SOKODU North	22
318	SOKODU South	22
318	KOBUIN	23

# Modelling choices:

## Explore and choose final survey data model

### Different coefficients specifications

- Individual, Aggregate and Individual + Aggregate level covariates

### Different random error specifications

Random intercepts? Random Slopes? At what levels?

### Assess the model fit

- E.g. Individual-level Logistic regression: Pseudo  $R^2$ , Sensitivity, Sensibility, AIC, BIC
- E.g. Multilevel Logistic regression: above + WAIC, Loo (Vehtari et al, 2016)

### Reproduce direct estimates

Can you survey model reproduce accurate poverty rates at regional level (using survey data)?

# Validation

- After you have used your survey model to predict poverty in Census cases and produced small area estimates there are still a few checks you need to carry out
- Can you reproduce direct survey poverty estimates using Census predicted values?
- Variation of your estimates (see Molina and Rao, 2010)
- Leave one variable out of your independent variables set to validate your small area estimates. Ideally use auxiliary data.

# Summary of a simple SAE workflow

## ➤ Pre-modelling choices:

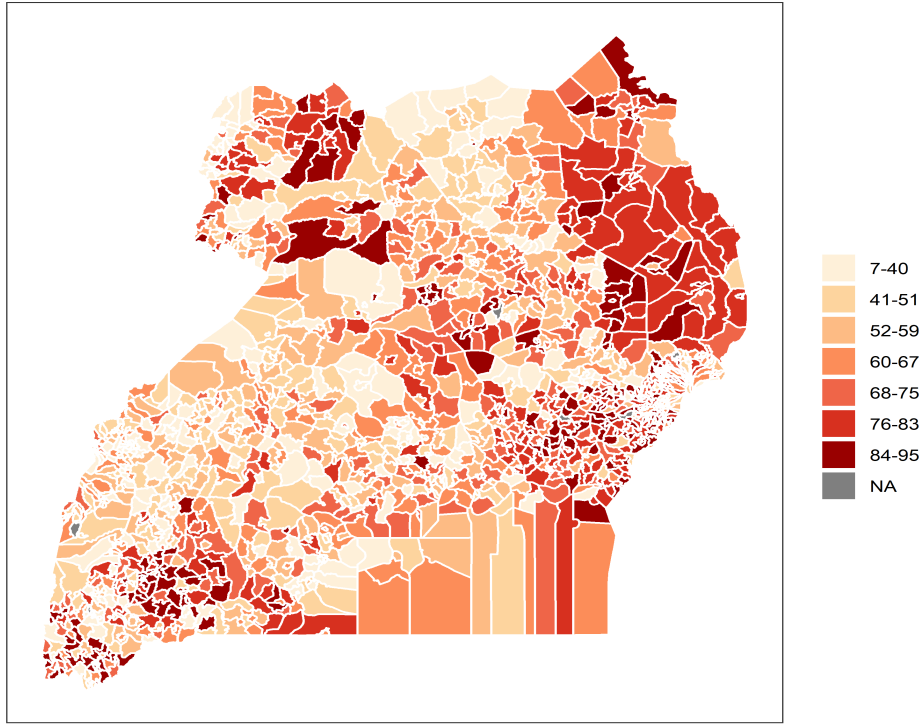
- Which small area?
- Survey and Census data Comparison
- Boundaries

## ➤ Modelling choices: Explore, compare and choose final survey data model

## ➤ Apply survey model to Census (predict poverty status of Census respondents) and produce Small Area Estimates

## ➤ Validate

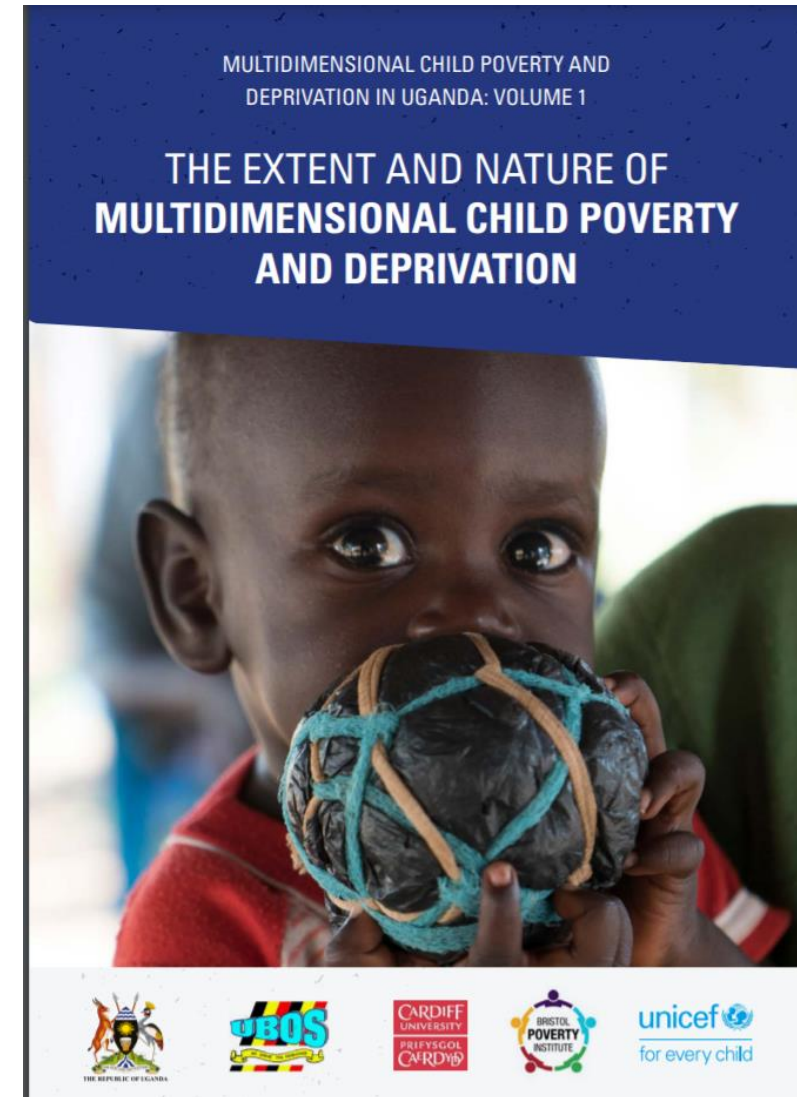
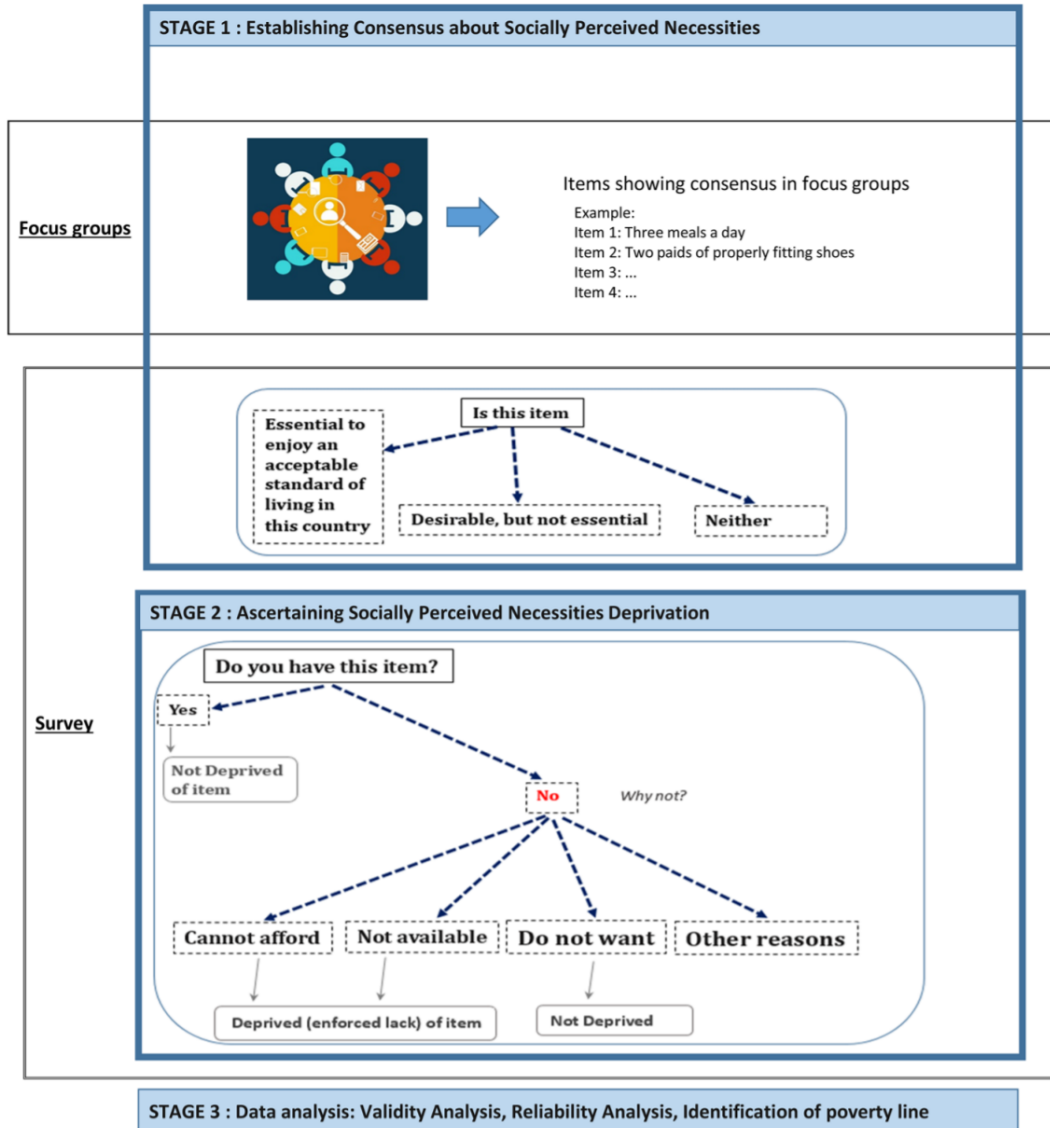
% of children in multidimensional poverty (Subcounty SAE Estimates)



# Applied example

Sub-county estimates of multidimensional poverty in Uganda 2016

# Multidimensional poverty in Uganda



**Table 2.5** Final child deprivation index components

<i>Relevant age range</i>	<i>Item</i>
0-17	A visit to the health facility when ill and all prescribed medication
0-17	Three meals a day
0-17	Two sets of clothing
0-17	Toiletries to be able to wash everyday
6-17	All fees, uniforms of correct size, and equipment
0-17	Own blanket
0-17	Own bed
0-17	Two pairs of properly fitting shoes
11-17	Own room for children over 10 of different sexes
3-17	Books at home for their age
0-17	Some new clothes
6-17	To be able to participate in school trips
6-17	Bus/taxi fare or other transport
6-17	A desk and chair for homework
6-17	Presents for children once a year on special occasions
3-12	Educational toys and games
0-17	To be able to make regular savings for emergencies
0-17	Repair a leaking roof for main living quarters
0-17	Repair or replace any worn out furniture
0-17	Replace broken pots and pans for cooking
0-17	Take children to a medical facility when sick
0-17	Pay school fees for children

# Pre-modelling choices

Uganda National Household Survey 2016/17 → Uganda Census 2014

➤ Pre-modelling choices:

- **Which small area?** Sub-county nationally and parishes for Kampala
- **Survey and Census data Comparison**
  - Applied post-stratification to UNHS 2016 (under-representation of rural households in the survey)
  - Inconsistent definition of household size and household head across two datasets (variables flagged/excluded)
- **Boundaries:** Region > sub-region > district > county > sub-county > parish > enumeration area . Several administrative changes, many days spent harmonising shapefile, Census and survey boundaries.



# Modelling choices: Explore, compare and choose final survey data model

- Started with basic individual logistic regression nested models
- Candidate set of independent variables draws on previous literature and advice from UBOS
- Led to final set of fixed effects

Logistic regression models predicting individual-level poverty status. Log-odds	
	Model 1
Urban	-0.15 *
clothes deprivation	0.29 **
shoes deprivation	1.33 ***
roof deprivation	0.29 ***
wall deprivation	0.44 ***
Sanitation type (Flush toilet)	
Latrine	1.59 ***
Covered pit latrine	2.55 ***
Covered pit latrine with a slab	3.02 ***
Covered pit latrine without a slab	2.60 ***
Uncovered pit latrine with a slab	3.29 ***
Uncovered pit latrine without a slab	2.13 *
No facility	3.39 ***
Other	4.28 ***
tv deprivation	1.59 ***
Improved water	0.16 *
Number of children	0.27 ***
Overcrowding	0.52 ***
bicycle deprivation	0.74 ***
Household head working in subsistence agriculture	
Household head Illiterate	
N	15646
Nagelkerke R2	0.32
Specificity	0.75
Sensitivity	0.75

# Modelling choices: Explore, compare and choose final survey data model

We then moved to multilevel modelling using Hierarchical Bayes Logistic Regression models

- Model 1 without including Sub-region-level intercepts.
- Model 1 + household head working in subsistence agricultural activities + household head working in subsistence agricultural activities (variables previously flagged as problematic)
- Model 1 + sub-region intercepts.
- **Model 1 + random intercepts at the district level**
- Model 1 + random slopes at the district level

# The final survey model

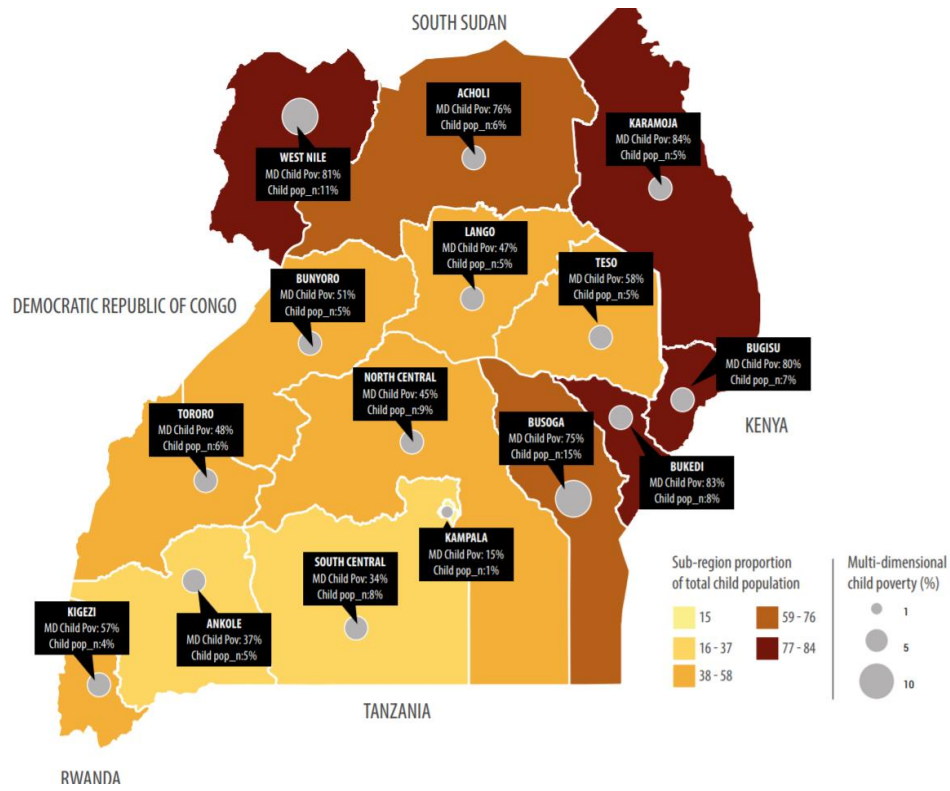
## - Model 1 + random intercepts at the district level

- Statistical fit: the WAIC (widely applicable information criterion) statistic of fit and Loo (leave-one-out cross-validation for fitted Bayesian models).
- Capacity to reproduce the subregional point estimates, i.e. whether the model reproduces the observed data (design estimates of multidimensional poverty).

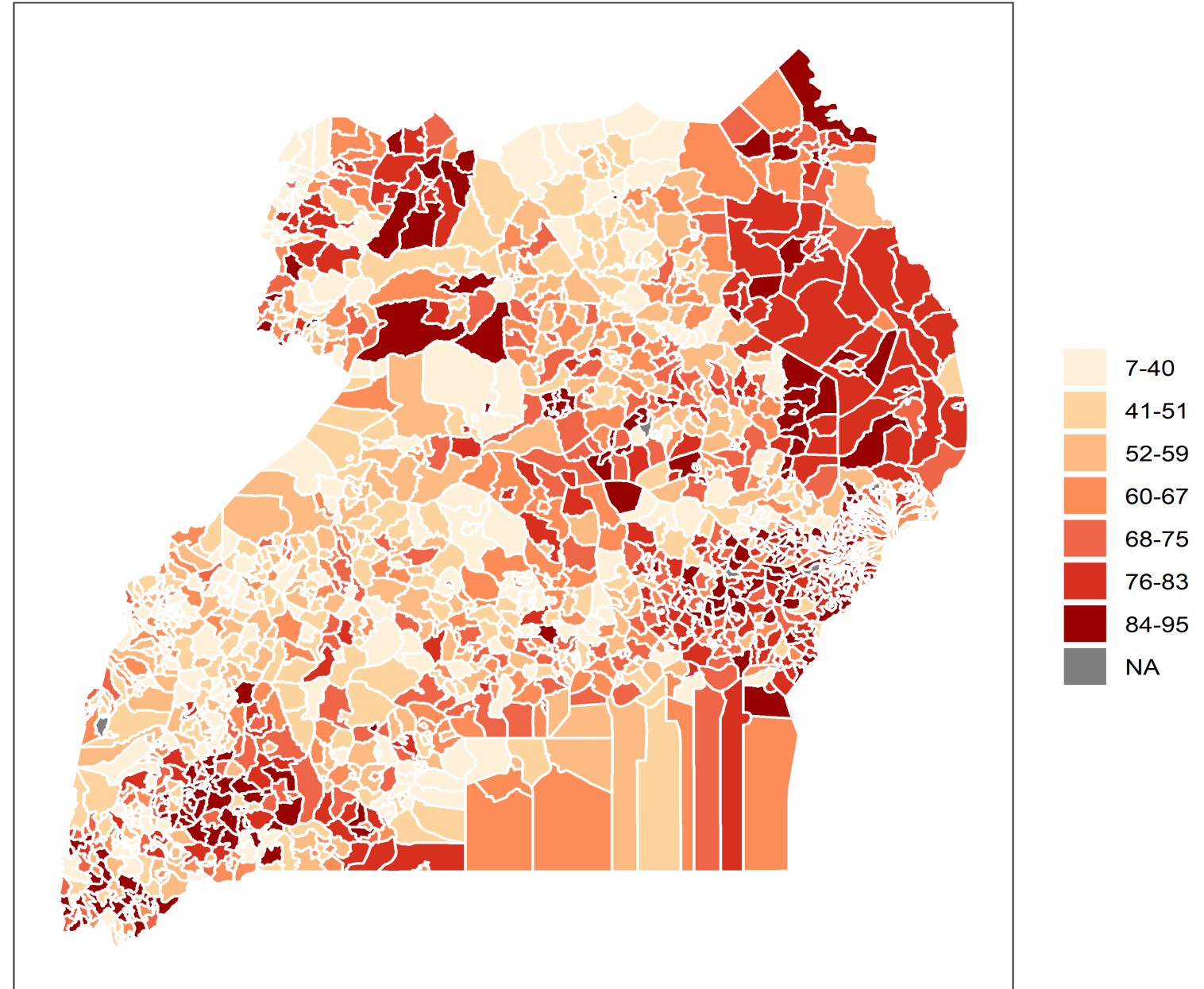
# Validation

% Poor (multidimensional poverty)

SubRegion	Survey direct estimate	Survey: Model prediction	Census: Model Prediction
Kampala	9 [6-11]	9	8
Central 1	27 [24-29]	27	27
Central 2	38 [34-41]	38	39
Busoga	59 [56-63]	60	59
Bukedi	74 [69-78]	74	74
Bugishu	63 [59-68]	63	64
Teso	53 [49-57]	53	52
Karamoja	75 [70-80]	75	75
Lango	42 [39-46]	42	42
Acholi	61 [57-65]	61	59
Westnile	70 [66-74]	70	72
Bunyoro	41 [37-45]	41	41
Tooro	41 [37-45]	41	39
Ankole	29 [25-34]	29	31
Kigezi	50 [44-55]	50	52



% of children in multidimensional poverty (Subcounty SAE Estimates)



# Findings for Uganda 2016 (forthcoming)

- Areas in the north, particularly in the north east, tend to have very high multidimensional poverty rates (Above 60%).
- However, there are pockets of high poverty in subregions that do not appear to have very high poverty rates at sub-region level
- Areas with the highest levels of need are also those with the lowest levels of infrastructure

# Conclusion

- Spend time making sure that shapefiles are compatible across datasets



- Use statistical software that can easily handle several types of datasets at the same time (e.g. R, Python)
- Avoid relying on pre-packaged SAE functions (e.g. try to understand the process yourself)
- Importance of auxiliary information for cross-validation
- Importance of relevant small area



# Acknowledgments

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